Shape-induced obstacle attraction and repulsion during dynamic locomotion

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Abstract

Robots still struggle to dynamically traverse complex 3D terrain with many large obstacles, an ability required for many critical applications. Body–obstacle interaction is often inevitable and induces perturbation and uncertainty in motion that challenges closed-form dynamic modeling. Here, inspired by recent discovery of a terradynamic streamlined shape, we studied how two body shapes interacting with obstacles affect turning and pitching motions of an open-loop multi-legged robot and cockroaches during dynamic locomotion. With a common cuboidal body, the robot was attracted towards obstacles, resulting in pitching up and flipping-over. By contrast, with an elliptical body, the robot was repelled by obstacles and readily traversed. The animal displayed qualitatively similar turning and pitching motions induced by these two body shapes. However, unlike the cuboidal robot, the cuboidal animal was capable of escaping obstacle attraction and subsequent high pitching and flipping over, which inspired us to develop an empirical pitch-and-turn strategy for cuboidal robots. Considering the similarity of our self-propelled body–obstacle interaction with part–feeder interaction in robotic part manipulation, we developed a quasi-static potential energy landscape model to explain the dependence of dynamic locomotion on body shape. Our experimental and modeling results also demonstrated that obstacle attraction or repulsion is an inherent property of locomotor body shape and insensitive to obstacle geometry and size. Our study expands the concept and usefulness of terradynamic shapes for passive control of robot locomotion to traverse large obstacles using physical interaction. Our study is also a step in establishing an energy landscape approach to locomotor transitions.

Keywords

Obstacle traversal, contact, physical interaction, potential energy landscape, morphological computation, cockroach, terradynamics

1. Introduction

Mobile robots are on the verge of becoming a major part of society. Many important applications, such as search and rescue, environmental monitoring, and extraterrestrial exploration, require robots to move through terrain with many obstacles comparable to or larger than the robot’s size. Robot locomotion in such complex 3D environments commonly relies on obstacle avoidance (Borenstein and Koren, 1991; Khatib, 1986; Rimon and Koditschek, 1992). The idea is to use sensors to obtain a geometric map of the environment (Dissanayake et al., 2001; Elfes, 1989), estimate the robot’s location and pose (Dissanayake et al., 2001; Leonard and Durrant-Whyte, 1991), treat large objects other than relatively flat ground (for terrestrial locomotion) as obstacles, plan a collision-free trajectory around them (Borenstein and Koren, 1991; Khatib, 1986; Lavalle, 1998), and control (Latombe, 2012) the robot to follow the trajectory. This approach is successful in structured (e.g., vacuum robots in organized rooms) (Tribelhorn and Dodds, 2007) and even dynamic (e.g., self-driving cars in traffic) (Thrun et al., 2000) environments, where obstacles are sparse, high-fidelity sensing and online computation is practical, and locomotor–ground interaction is well understood and readily controlled (Bekker, 1956; Pacejka, 2005; Wong, 2008).

However, obstacle avoidance using environment geometry fails for dynamic locomotion in highly cluttered, complex 3D terrain, where many of the above steps fail. First, a collision-free trajectory to reach the goal simply may not
exist. In addition, many existing methods of localization, state estimation, planning, and control of robot locomotion only work well for slow, quasi-static, kinematic movement (Arslan and Saranli, 2012). By contrast, inevitable, continual dynamic interaction of the robot with cluttered large obstacles (Gart et al., 2018; Gart and Li, 2018; Li et al., 2015; Qian et al., 2019; Rieser et al., 2019; Transeht et al., 2008) induces frequent large perturbations and uncertainty in motion and sensing (Garcia Bermudez et al., 2012; Ordonez et al., 2013) or even results in flipping over (Guizzo and Ackerman, 2015; Li et al., 2016), making these methods impractical. Furthermore, existing locomotor–ground interaction models (e.g., tire dynamics for paved roads (Pacejka, 2005), terramechanics for deformable off-road terrain (Bekker, 1956; Wong, 2008)) do not apply to cluttered terrain.

Biologically inspired multi-legged robots hold the promise for robustly traversing cluttered terrain, with inherent advantage of legs in overcoming large obstacles (Raibert, 2008) and higher stability offered by multiple legs (Full et al., 2006; Ting et al., 1994). By exploiting natural dynamics of leg–ground interaction (Childers et al., 2016; De and Koditschek, 2018; Garcia Bermudez et al., 2012; Li et al., 2009; Qian and Koditschek, 2020; Raibert, 2008; Saranli et al., 2001; Spagna et al., 2007) and body–terrain interaction (Gart et al., 2018; Gart and Li, 2018; Li et al., 2015), multi-legged robots have achieved improved locomotor performance and capabilities in complex terrain compared to those using quasi-static planning and control (although still far from robust (Arslan and Saranli, 2012)). For example, a recent study empirically discovered that an ellipsoidal body shape helps traverse cluttered obstacles by inducing body rolling through gaps narrower than the body width (Li et al., 2015).

Inspired by the critical role of shape to align parts in robotic manipulation (Peshkin and Sanderson, 1988), here we take the next step in understanding how shape affects body–obstacle interaction during dynamic locomotion. We experimentally tested and compared how two body shapes, cuboidal and elliptical, affect pitching and yawing motions (Section 2), useful for initiating climbing and turning. Multi-legged robots (Figure 1) typically have a cuboidal body shape (Figure 2A, top), whereas an elliptical body shape (Figure 2A, bottom) is rarely used by robots. For simplicity, we chose rigid vertical pillars as our model terrain (Figure 2), representative of large immovable obstacles common in cluttered terrain. To further test the effect of obstacle geometry, we used pillars of circular and square cross-sectional shapes and varied their orientation. To understand to what extent traversal can be achieved using passive interaction and when active adjustments must be made, we comparatively studied a RHex-class robot with open-loop control and insects capable of sensory feedback (Figure 2). We chose the forest-floor-dwelling discoid cockroach (Figure 2B) that is exceptional at traversing cluttered obstacles such as dense vegetation and leaf litter (Bell et al., 2007). We studied the animal’s locomotion during rapid escape response where passive mechanics dominates (Dickinson et al., 2000; Full and Koditschek, 1999; Sponberg and Full, 2008) to allow closer comparison with the open-loop robot.

For both the robot and animal, we discovered that a cuboidal body shape induces attraction towards the obstacle whereas an elliptical body shape induces repulsion away from the obstacle (Figure 3); however, both are surprisingly insensitive to obstacle geometry (Section 3). Inspired by the similarity of physical interaction and usefulness of quasi-static potential energy models for explaining shape-dependent physical interaction in robotic part alignment and grasping without force closure (Brost, 1992; Jayaraman, 1996; Zumel, 1997), we developed a similar potential energy landscape model to explain the sensitive dependence of dynamic interactions on body shape and further generalize our finding to more body shapes and obstacle sizes (Sections 4 and 5). The model well explained the observed dependence of physical interaction on body shape and the resulting stochastic dynamic locomotion. In addition, it revealed that interaction is insensitive to obstacle geometry and size and that attractive interaction stems from the body’s frontal flatness. We demonstrated the usefulness of shape-induced obstacle repulsion and attraction for passive control of dynamic locomotion in complex terrain by eliciting desired locomotor transitions (Section 6). Finally, we discuss broader implications for robotics and future directions (Section 7).

We note that our work is an advancement over the previous study (Li et al., 2015) in several aspects. First, this work expands the concept of terradynamic shapes, from an ellipsoidal body shape that induces body rolling into obstacle gaps, to cuboidal and elliptical body shapes that induce obstacle attraction and repulsion. These different physical interactions are useful for eliciting distinct locomotor transitions. In addition, the previous study did not study how body–obstacle interaction depends on obstacle shape, orientation, and size. Here, we discover that obstacle attraction or repulsion is an inherent property of the locomotor body shape and is insensitive to obstacles. Furthermore, although the previous study introduced an early potential energy landscape model, in order to explain the observed dependence of body orientation on body shape during obstacle interaction, it assumed that the system is always in its minimal potential energy state over rotational degrees of freedom. However, it is not clear whether this is true for a self-propelled, dynamically moving robot or animal. By quantifying 3D kinematics and reconstructing body–obstacle interaction, our study reconstructs how the system behaved on the potential energy landscape. We demonstrate that, although the self-propelled system does not reach minimal potential energy orientation, it is strongly attracted to it, explaining why the quasi-static potential energy landscape is useful in understanding dynamic locomotion.
2. Experimental methods

2.1. Robot experiments

We built a RHex-class robot for experiments (Saranli et al., 2001). We attached six servo motors with embedded velocity PD controllers to the chassis to drive six 3D-printed S-shaped legs (PLA plastic) in an alternating tripod gait (leg rotation frequency = 1 Hz). We chose S-shaped legs to double effective step frequency over the original C-shaped legs of RHex. To increase ground traction, we wrapped legs with duct tape and covered the robot obstacle track with sandpaper (60 grit size). We attached a 3D-printed elliptical or cuboidal shell to its dorsal surface (Figure 2A). Because we could precisely control robot trajectory when approaching obstacles, we simply used a single pillar to study robot-terrain interaction. We parameterized square pillar orientation using the angle between its left/right side and the forward (+x) direction and chose it to be 0°, 30°, and 60° (Figure 2A). We started the robot at a constant initial fore–aft distance (50 cm between the robot marker and pillar center) moving at a speed of 30 cm s⁻¹, with an initial direction aligned with the x-axis. We varied initial lateral offset $y_0$ (0, 3, 6, 9, and 12 cm) to vary initial bearing (Figure 2A). For each pillar shape and orientation, we collected 25 trials, with 5 trials for each initial bearing. See Table S1 in the supplementary information for sample size, mass, and dimensions of robot experiments.

2.2. Animal experiments

We used ten healthy male discoid cockroaches (*Blaberus discoidalis*), as females were often gravid and under different load-bearing conditions. Prior to experiments, we kept the animals in individual plastic containers at room temperature (22°C) on a 12 h:12 h light:dark cycle and provided dog food and water *ad libitum*. We attached an elliptical or a cuboidal shell to the animal's dorsal surface (Figure 2B) using hot glue after trimming the wings. The shells were vacuum formed from 0.05 cm thick polystyrene sheets. Because the animal rarely collided if only a single pillar was present, we constructed an obstacle field with a row of seven rigid aluminum pillars which were press-fit vertically onto an acrylic sheet (Figure 2B). The circular pillars (Figure 2B, top) had a diameter that equals the side length of square pillars (Figure 2B, bottom). The lateral spacing between two adjacent pillars was only 10% larger than the animal shell width. We did not vary square pillar orientation as in robot experiments, as natural animal motion already varied it. We tested 10 animals for each body shape and used the same group of animals for different pillar shapes and orientations. For each trial, we placed the animal at one end of the track and pressed its abdomen to induce it to traverse the pillars. The animal was then allowed to rest in a shelter at the opposite end of the track for at least 1 minute. Animal experiments were conducted at 40°C. See the supplementary information, Table S2, for sample size, mass, and dimensions in animal experiments.

We verified that during a rapid escape response the animal's body–pillar initial obstacle interaction was dominated by passive mechanics with minimal active sensory feedback (supplementary information Section S3 and Figure S3).
2.3. 3D kinematics reconstruction

We recorded robot and animal experiments at 100 frames s⁻¹ and a resolution of 2,560 × 2,048 pixels using four synchronized, calibrated cameras from top views with different orientations (Figure 2). To automatically track the body in all camera views, we attached a BEEtag marker (Crall et al., 2015) to the dorsal face of the shell. We then reconstructed 3D kinematics of marker using direct linear transformation (Hedrick, 2008) and calculated the body’s 3D position (x, y, z) relative to the pillar and 3D orientation (Euler angles: yaw, pitch, and roll). We identified the phases of the trial when body was in contact with the obstacle, by creating a CAD model of the shell and reconstructing its motion relative to the pillar(s) using 3D kinematics calculated above. See supplementary information Section S1 for details of imaging and reconstruction.

2.4. Data analysis

We focused on the physical interaction at the first pillar contacted by the robot or animal. To simplify quantification of continual body–obstacle interaction composed of many small high-frequency collisions (supplementary information Section S4), we defined the interaction phase as the portion of the trial during which the body had sustained continual collisions. This begins when the body’s front face (curved vertical face for elliptical body) came within a small distance (animal 1.5 mm; robot 2 mm) of the pillar and ends when this distance exceeded 5 mm or when the body collided with a second obstacle (whichever occurred sooner). We compared recorded and 3D reconstructed videos to verify that this definition well matched the visually observed beginning and ending of the interaction in all trials, and we found them to be accurate to within 10 ms. All following analyses of body–obstacle interaction are for this continual interaction phase.

To quantify turning and pitching during interaction, we defined the following metrics. We defined body bearing (θ) relative to the pillar as the angle between the body midline and the line connecting body geometric center and pillar center in the x–y plane (Figure 4A). Initial bearing θ₀ was the value when the body first contacted the pillar. Final bearing θ_f was the value when the body maximally turned away or towards the pillar relative to its initial bearing (Figure 4C and D, filled blue and red dots). Similarly, we defined initial pitch (ϕ₀) as the body pitch angle when the body first contacted the pillar (Figure 5A) and maximal pitch increase Δϕ_max (Figure 5C and D, blue and red arrows) as the difference between the maximal and initial values.

For the animal, we rejected trials in which the animal did not contact any pillar or contacted the sidewall before contacting any pillar. We also rejected trials in which animal interacted with the first pillar for less than 0.03 s before contacting a second pillar because, when interaction was too short, the initial dynamic collision and body oscillation due to leg–ground interaction dominated motion. With these criteria, we accepted ~5 trials for each animal with each body shape and pillar shape and orientation treatment. We defined transition probability for both the robot and animal as the percentage of trials in which a locomotor mode or outcome occurs among all accepted trials. Note that it is not the same as transition probability of a Markov chain. See supplementary information Tables S1 and S2 for sample size of accepted trials and Section S2 for statistical tests.

3. Experimental results

3.1. Traversal probability depends on body but not obstacle shape

With a cuboidal body, both the robot and animal had a low traversal probability. The robot never traversed the circular pillar (Figure 3A), and the animal only traversed about once every three times (Figure 3C). By contrast, with an elliptical body, both the robot and animal had a high traversal probability (Figure 3B and D). Surprisingly, traversal probability of both the robot and animal did not significantly change with obstacle shape and orientation (Figure S4, P < 0.05, Kruskal–Wallis test). The difference in traversal probability between the two body shapes was mainly a result of the sensitive dependence of body turning and pitching on body shape, as elaborated in the following.

3.2. Turning depends sensitively on body shape

The cuboidal and elliptical body shapes resulted in distinct body turning directions (Figure 4). With a cuboidal body, the robot or animal was initially attracted to and turned towards the obstacle (Figure 3A and C, blue curve; Figure 4B, blue; supplementary Movie S1), with final bearing θ_f (see the definition in Figure 4C and D) almost always converging to zero for all θ (Figure 4C–F, blue). Although the robot’s bearing often overshot after aligning with the obstacle (θ = 0°), it was always attracted back and oscillated around the obstacle (Figure 4C, blue; supplementary Movie S1). The animal, however, rarely oscillated after aligning with the obstacle but often continued to turn away until it traversed the obstacle (Figure 3C, yellow; Figure 4D, blue; supplementary Movie S1), with continual leg pushing and slipping and occasional body rolling. By contrast, with an elliptical body, the robot or animal was quickly repelled and turned away from the obstacle (Figure 3B and D, red curve; Figure 4B, red; supplementary Movie S1), with θ_f almost converging to 90° for the robot for all θ₀ and increasing with |θ₀| for the animal (Figure 4C–F, red). After turning away from the first pillar, the animal...
was sometimes deflected by other pillars (Figure 3C and D, gray arrow) and did not traverse.

3.3. Pitching depends sensitively on body shape

Body shape strongly affected body pitching during interaction for both the robot and animal (Figure 5). With a cuboidal shape, as the body turned towards the obstacle (Figure 4B) and legs continued to propel, the body often pitched up (Figure 3A, C, blue curve; Figure 5C, D, blue; supplementary Movie S1). The robot always pitched up (Figure 3A, blue) to a nearly vertical body orientation (Figure 5B, solid blue bar) and eventually flipped over (Figure 3A, black). The animal, however, after initially pitching up (Figure 3C, blue), always managed to turn sideways to escape (Figure 3C, yellow) before it could pitch up further and thus never flipped over. As a result, the robot’s maximal pitch increase $\Delta \phi_{\text{max}}$ (defined by arrows in Figure 5C and D) was higher than that of the animal (Figure 5B, blue; $P < 0.001$, Kruskal–Wallis test). By contrast, with an elliptical shape, as the body was repelled away from the obstacle, $\Delta \phi_{\text{max}}$ was significantly smaller (Figure 5B, red; Figure 5E and F; supplementary Movie S1) than that with a cuboidal body ($P < 0.001$, Kruskal–Wallis test).

For a cuboidal body, after turning towards the obstacle, large pitching occurred stochastically: the time required for the body to pitch up significantly after initial contact was highly variable from trial to trial (Figure 5C and D). In some trials, this happened as soon as the body first aligned with the obstacle; in others, this happened after body bearing oscillated several times (Figure 4C and D).

For both the robot and animal with a cuboidal body, we did not find a significant dependence of $\Delta \phi_{\text{max}}$ on $|\theta_0|$ (Figure 5E and F, blue; $P > 0.05$, Kruskal–Wallis test). By contrast, for both the robot and animal with an elliptical body, $\Delta \phi_{\text{max}}$ decreased with $|\theta_0|$ during interaction (Figure 5E and F, red; $P < 0.001$, Kruskal–Wallis test).
3.4. Turning and pitching are insensitive to obstacle geometry

Surprisingly, for both the robot and animal, turning and pitching motions were similar for all obstacle shapes and orientations tested (Figures S5 and S6), with no significant difference in final bearing and pitch increase ($P > 0.05$, Kruskal–Wallis test; Figures 4E and F and 5E and F). Final bearing of elliptical robot (Figure 4E, red) showed a weak dependence on pillar shape ($P = 0.004$, Kruskal–Wallis test) and orientation ($P = 0.02$, Kruskal–Wallis test) but only varied within 2% (mean ± s.d. = 94° ± 2°). This insensitivity is particularly remarkable for the open-loop robot (supplementary Movie S2), whose data for different pillar shapes and orientations collapsed onto a straight line (Figures 4E and 5E).

4. Modeling methods

4.1. Rationale for potential energy landscape model

For both the robot and animal, body–obstacle interaction consisted of continual collisions due to cyclic self-propulsion (supplementary material Section S4). Although such complex, noisy dynamics can in principle be solved (e.g., using multi-body dynamics simulation (Xuan and Li, 2020b)), such modeling is more like doing an in silico experiment and may become intractable. Inspired by similarities of our system to robotic grasping, here we chose to use a quasi-static potential energy landscape model to explain how body shape induces obstacle attraction and repulsion during dynamic locomotion, without solving for the dynamics.

Our system is similar to many problems in robotic manipulation (e.g., part alignment (Boothroyd and Ho, 1976; Brost, 1992; Jayaraman, 1996; Peshkin and Sanderson, 1988; Várkonyi, 2014), grasping without force closure (Lynch et al., 1998; Lynch and Mason, 1999; Zumel, 1997)) in that shape strongly affects physical interaction. In addition, in robotic part alignment, motion also consists of continual collisions (Jayaraman, 1996; Mohri and Saito, 1994; Peshkin and Sanderson, 1988; Zumel, 1997). Despite this, quasi-static potential energy field models well explained how part and feeder shapes affect their interactions and informed planning strategies to achieve the desired alignment even with uncertainties in part orientation, friction, and intermittent contact dynamics (Brost, 1992; Peshkin and Sanderson, 1988; Zumel, 1997).

4.2. Model approximations and definition

Our potential energy landscape (Figures 6–8) directly results from physical interaction (similar to Mason et al., 2012) and is unlike artificial potential fields (Khatib, 1986) or navigation functions (Rimon and Koditschek, 1992) (Figures 6–8). Our model had several simplifying assumptions and approximations. First, we approximated both the locomotor body and obstacle as a rigid body and neglected legs, which rarely contacted the obstacle during interaction. Second, we chose to focus on pitch and bearing (turning) and constrained body roll to be zero considering that it was small during interaction (Figure S2). In addition, we assumed that the body’s lowest point always contacted the ground. Furthermore, the potential energy landscape only modeled the effect of conservative gravitational force. Moreover, we neglected dynamics of the system; thus, prediction of robot’s trajectories in dynamic motion is not possible.
The potential energy of the system was \( E = mgz \), where \( m \) was body mass, \( g \) was gravitational acceleration, and \( z \) was the body’s center of mass height. For each body horizontal position \((x, y)\) relative to the obstacle, center of mass height and thus potential energy were determined by body pitch and bearing. To obtain the potential energy landscape, we first determined center of mass position and orientation from the reconstructed 3D motion. For each center of mass position \((x, y, z)\) along the measured trajectory of a trial, we calculated body potential energy as a function of body pitch and bearing by rotating the body about a pitch and a yaw axis through the center of mass. We normalized potential energy to that when body pitch was zero, \( mgz_0 \), where \( z_0 \) is center of mass height when body is horizontal (pitch and roll are both zero).

4.3. Model analysis of intermediate shapes
To better understand what aspect of body shape induces obstacle attraction and further examine whether there was a critical intermediate body shape between elliptical and cuboidal shape where body–obstacle interaction changed from attractive to repulsive, we calculated the potential energy landscape of superellipses, given by

\[
\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 1
\]

where \(2a\) and \(2b\) are body length and width, respectively, and \(n\) parametrizes the shape \((n = 2 \text{ for ellipse and } n = \infty \text{ for rectangle})\). We varied \(n\) in the range \([2, 20]\) in increments of 0.25 to create superellipses and extruded them by the body height \(2c\) (Figure 9A). For simplicity, we assumed constant zero bearing. We then moved the body towards the pillar and calculated the potential energy landscape (Figure 9B–D, supplementary Movie S7), as described in Section 4.2. We assumed the same mass and uniform mass distribution for all body shapes.

5. Modeling results
5.1. Potential energy landscape topology differs between body shapes
Before the body contacted the obstacle, the potential energy landscape was the same for the cuboidal and elliptical bodies (Figure 6A and D). Potential energy only increased with body pitch and did not change with bearing. When the body was sufficiently close to the obstacle, it must pitch up and/or turn; otherwise, it would penetrate the rigid obstacle, resulting in infinite potential energy (Figure 6B and E, white). The boundary of the infinite potential energy regions in the landscape represented all possible pitch and bearing states with contact. Hereafter, we refer to these as prohibited regions. As the body moved even closer, it had to turn and/or pitch up more, and the prohibited regions became larger (Figure 6C and F, white).

For the cuboidal body (supplementary Movie S3), as it moved close to the obstacle, two prohibited regions emerged (Figure 6B and C, white), with two saddle points corresponding to frontal bottom corners of the body contacting the obstacle. The inner boundary of prohibited regions between the saddle points corresponded to when the body contacted the obstacle in the front. The outer boundaries beyond the two saddle points corresponded to when the body contacted the obstacle on the sides. When the body contacted the obstacle in the front, body pitch increased with bearing magnitude, i.e., the body must pitch up to turn away from the obstacle. For the elliptical body close to the obstacle (supplementary Movie S4), only one prohibited region emerged (Figure 6E and F, white), centered around zero bearing. The curved boundary of the prohibited region corresponded to when the body contacted the obstacle, with the single saddle point being in contact in the front middle. With contact, the body pitch decreased with bearing magnitude, i.e., the body pitched down as it turned away from the obstacle.

The different shapes of prohibited regions between the two body shapes resulted in different topologies of attractive basins of the landscape (Figure 6B and C versus Figure 6E and F; supplementary Movie S3 versus supplementary Movie S4). For the cuboidal body, there existed a local minimum basin at zero body pitch around zero bearing between the prohibited regions and two basins at zero body pitch at large body bearing magnitudes beyond the prohibited regions. For the elliptical body, only the latter existed. Hereafter, we refer to the former as the turn-towards-and-pitch basin and the latter as the turn-away basins.

5.2. Model explains dependence of turning and pitching on body shape
The distinct topology of attractive landscape basins between the cuboidal and elliptical shapes provided insight into why they resulted in the observed motions. A static body contacting an obstacle can be stable in any orientation as long as friction against the ground and obstacle is sufficient. However, for the self-propelled robot or animal, continual collisions during obstacle interaction (Figure S1) broke continuous frictional contact and caused the body to be statically unstable. As a result, the system drifted from less-stable (higher-energy) to more-stable (lower-energy) states on the potential energy landscape, i.e., it was attracted to landscape basins.

As the cuboidal body moved closer to the obstacle, the turn-towards-and-pitch basin remained around zero bearing but shrank in the bearing direction and moved up in the positive pitch direction (Figure 6B and E, supplementary Movie S3). As a result of this attractive basin, when the cuboidal body continued to self-propel against the obstacle in the front, it turned towards the obstacle and then pitched up. By contrast, as the elliptical body moved closer, the
two pitch-away basins moved away from zero bearing but did not in the pitch direction (Figure 6E and F, supplementary Movie S4). As a result of these two attractive basins, when the elliptical body continued to self-propel against the obstacle in the front, it was repelled away while staying around zero pitch. These findings in self-propelled, dynamic locomotor–obstacle interaction are similar to how feeders are shaped appropriately to trap or reject parts (Brost, 1992; Caine, 1993; Jayaraman, 1996; Peshkin and Sanderson, 1988) and how part shape probabilistically affects its resting orientation when dropped on a feeder (Boothroyd and Ho, 1976; Varkonyi, 2016).

Indeed, the ensemble of system state trajectories from experiments (Figure 7, supplementary Movies S5 and S6) showed that, despite the drastic simplification, our potential energy landscape model well explained the dynamic motion of the system resulting from complex, noisy interaction (Figure S1). With a cuboidal body, the system state in all trials was attracted towards the local minimum basin around zero bearing and then increased in pitch (Figure 7A

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**Fig. 6.** Potential energy landscape over body pitch and bearing. Results are shown for robot body interacting with circular pillars and are similar for animal (supplementary Movies S3 and S4), other pillar shapes and orientations (Figure S7), and pillars of large sizes (Figure 8). (A)-(C) A forward-moving cuboidal body interacting with obstacle results in a landscape that attracts it towards obstacle (bearing converges to zero), which then leads to pitching up. (D)-(F) A forward-moving elliptical body interacting with obstacle results in a landscape that repels it away from obstacle (bearing diverges from zero), with little pitching up. In (A)-(F), top panels show body position and orientation; the bottom panels show potential energy landscape. Landscape for negative pitch is symmetric to that of positive pitch and not shown for simplicity. Three snapshots of a representative trial are shown for each shape: (A), (D) before contact, (B), (E) shortly after contact, and (C), (F) as the body moves even closer to the obstacle. See supplementary Movies S3 and S4 for landscape evolution during interaction. The white region in a landscape encloses impossible states in which the body must penetrate a rigid obstacle, resulting in prohibited region(s); cyan dots and curves show current system state and state trajectory projected onto the landscape. Saddle points and local minimum/minima are shown. Blue or red arrows show the direction of potential energy gradient along boundary of prohibited regions.
With an elliptical body, the system state in all trials was repelled away from zero bearing by the expanding prohibited region (Figure 7B and D). One exception is that the passive model did not explain how the cuboidal animal escaped obstacle attraction, with system state going out of the attractive basin between the saddle points (Figure 7C). These quantitative measurements of state trajectories on the landscape also demonstrated that the self-propelled, dynamic system was strongly attracted to the basins but did not reach and stay at the lowest potential energy state. We note that the observed body turning may be intuitively explained by assessing the torque from body–pillar contact force (which should be approximately perpendicular to the local tangent of the body) in a simple planar model. However, we view potential energy landscape modeling as a general approach to locomotion in complex 3D terrain (Othayoth et al., 2020). For example, we can use it to study and understand how changes in body or terrain properties (e.g., body shape here, obstacle stiffness in Othayoth et al. (2020)) affect motion in three dimensions, by observing and analyzing how the system state behaved on a landscape over the relevant configuration space of that particular problem (e.g., body bearing and pitch here, body roll and pitch in Othayoth et al. (2020)).

5.3. Model explains insensitivity to obstacle geometry

For both body shapes, the potential energy landscapes from different obstacle shapes and orientations were strikingly similar (Figures 8 and S7). This explained why they did not affect traversal probability (Figures 3 and S4) and body turning (Figures 4 and S5) and pitching (Figures 5 and S6) motions. In addition, the potential energy landscapes from obstacles with a diameter comparable with or much larger than body size were also qualitatively similar (Figure 8). Together, these results demonstrated that obstacle attraction followed by pitching up, or obstacle repulsion with little pitching, is an inherent property of the self-propelled locomotor induced by body shape, regardless of obstacle geometry and size.

5.4. Model reveals obstacle attraction stems from frontal flatness of body

Our model analysis of intermediate shapes showed that obstacle attraction is mainly a result of the flatness of the front of the body and increases as the body becomes more cuboidal. As the body shape changed from elliptical \((n = 2)\) to cuboidal \((n > 2)\), Figure 9A(i)–(iii), supplementary Movie S7), the initially curved front face became increasingly flat in the middle. This led to a change in the number of attractive landscape basins, from not having the turn-towards-and-pitch basin to having it, which was insensitive to obstacle size (Figure 9B–D, supplementary Movie S7). Because the emergence of the turn-towards-and-pitch basin stems from the flatness of the front face, simply rounding the corners (such as in Spot from Boston
Dynamics) will not mitigate pitching up and flipping over for cuboidal robots.

We also found that the body shape at which the turn-towards-and-pitch basin emerged depended on body–obstacle distance. In other words, there is not a single “critical” shape that separates the repulsive and attractive regimes. As the body moved very close to the obstacle, all shapes tested became attractive (supplementary Movie S7). This appeared surprising for the elliptical body but was consistent with our experimental observations—the robot and animal were repelled to turn away from the obstacle before they could move so close to it.

6. Applications

6.1. Elliptical body enables open-loop traversal of cluttered obstacles

Our discovery of obstacle repulsion of an elliptical body is useful for passive control of dynamic traversal of cluttered obstacles without sensory feedback. To demonstrate this, we challenged our open-loop robot to traverse a multi-pillar field with narrow gaps (150% body width, pillars arranged in an equilateral triangle grid, Figure 10A and B, supplementary Movie S8), starting from different initial position and body yaw. With a cuboidal body (Figure 10A), the robot was continually attracted toward every obstacle that it contacted along its way. Thus, it was almost always trapped inside the obstacle field, rarely traversed (Figure 10C and D, blue), and often flipped over (53% probability within 8 seconds). By contrast, with an elliptical body (Figure 10B), the robot always traversed the field as it was continually repelled away by obstacles (Figure 10C and D, red). We also made similar observations in natural terrain cluttered with irregularly shaped boulders (Figure 10E and F, supplementary Movie S9, left; supplementary Movie S10, left). Although we only demonstrated this in a small obstacle field, it is almost certain that an elliptical shape can lead to traversal in much larger obstacle fields and could be useful even in aerial or aquatic locomotion (see supplementary material Sections S5, Figure S8, and Movie S13).

Fig. 8. Potential energy landscape from large obstacles. (A)–(E) Cuboidal and (F)–(J) elliptical robot body interacting with a large circular (A), (F) and square pillars oriented at 0° (B), (G), 30° (C), (H), and 60° (D), (I) relative to the x-axis, and with an infinitely large obstacle (E), (J). See Figure 6 for definitions of the plots.
6.2. Pitch-and-turn helps cuboidal robots escape obstacle attraction

To inform how cuboidal robots should escape obstacle attraction and avoid subsequent flipping over, we observed how the animal achieved this. After being attracted towards the obstacle (Figure 11A(i) and (ii)), the animal often first pushed both hind legs backwards to pitch its body up substantially against the obstacle (Figure 11A(iii)), then extended one hind leg while protracting the other (Figure 11A(iv)), presumably to generate a torque to turn its body away from the obstacle.

Similar to parts overcoming potential energy barriers to reach and remain in a potential energy local minimum state (desired orientation) (Boothroyd and Ho, 1976; Jayaraman, 1996; Varkonyi, 2016; Zumel, 1997), we can view the escape from obstacle attraction as a barrier-crossing transition on our potential energy landscape (Othayoth et al., 2020), escaping the turn-towards-and-pitch basin to reach the turn-away basins. To further understand why the animal pitched up before turning, we examined the potential energy landscape of a forward-moving cuboidal body pitching up against the pillar with a constant zero bearing (supplementary Movie S11). As the body moved closer and pitched up (Figure 11B versus Figure 11C), potential energy gradient \( \frac{dE}{d\theta} \) at the system state along the bearing direction decreased (Figure 11D). For a body in quasi-static equilibrium, this gradient was the torque exerted by body weight to turn the body towards the pillar. For the self-propelled animal (or robot), because continual collisions break continuous frictional contact, this torque may be similar in magnitude to the dynamically changing torque required to turn against the obstacle. Therefore, the decreasing gradient with increasing pitch suggested that, by pitching its body up, the animal reduced the turning torque required to initiate turning and escape obstacle attraction.

Inspired by these animal observations and modeling results, we designed a pitch-and-turn strategy to help cuboidal robots escape obstacle attraction more easily (supplementary Movie S12). As the robot approached and pitched up against a pillar obstacle using an alternating tripod gait (Figure 12A–C(i)–(iii)), we manually triggered the robot to lock its front and mid legs and rotate its hind legs in...
opposite directions to turn the body until it escaped (Figure 12A–C(iv)) and resumed the alternating tripod gait (Figure 12A–C(v)). In accord with the model prediction of reduced required turning torque with increased pitch (Figure 11C and D), the robot escaped if its body pitch exceeded a critical value (~40º) and otherwise failed to escape due to leg slipping and flipped over. Similarly, the robot traversed natural cluttered terrain using a series of manually triggered pitch-and-turn maneuvers (Figure 12D; supplementary Movies S9 (right) and S10 (right)). We emphasize that, although cuboidal robots could simply back up to escape obstacle attraction when obstacles are sparse, active gait change like this is required to traverse highly cluttered terrain (e.g., earthquake rubble).

7. Discussion

Our study expands the new concept and usefulness of terradynamic shapes (Li et al., 2015) and is a step in establishing terradynamics (Li et al., 2013) of locomotion in complex 3D terrain (Gart et al., 2018, 2019; Gart and Li, 2018; Li et al., 2019; Qian and Koditschek, 2020). We provide new principles of how robots should use body shape to induce obstacle attraction and repulsion to passively control dynamic locomotion. A self-propelled cuboidal body induces attraction towards an obstacle and subsequent pitching up against it, which hinders obstacle traversal but may be useful for initiating climbing. By contrast, a self-propelled elliptical body is repelled away by obstacles and enables rapid traversal without feedback control or planning. This is particularly useful for small robots in time-sensitive or payload-limited missions such as search and rescue (Murphy et al., 2008) or extraterrestrial exploration (Bajracharya et al., 2008). More broadly, adopting the right body shape can change the topology of attractive landscape basins and suppress unfavorable locomotor modes. This added to the suite of strategies that robots and animals can use to elicit the desired motions (Gart and Li, 2018; Li...
Fig. 11. Pitching up against an obstacle facilitates escape of a cuboidal body from obstacle attraction. (A) Snapshots of a cuboidal animal escaping after being attracted towards obstacle. Blue and yellow arrows show motions defined in Figure 3. White and cyan arrows show hind leg extension and protraction. (B), (C) Potential energy gradient $dE/d\theta$ (red arrow) along bearing direction when body contacts pillar in the front middle (cyan dot) for low (B) and high (C) body pitch, with constant zero bearing. (D) Potential energy gradient $dE/d\theta$ as a function of body pitch, with constant zero bearing. Here $w$ is the half-distance between hind legs. Cyan markers show values of $dE/d\theta$ from (B) and (C). See supplementary Movie S11 for evolution of landscape and gradient.

Fig. 12. Pitch-and-turn strategy helps cuboidal robots escape obstacle attraction. (A) Snapshots of a cuboidal robot using pitch-and-turn strategy to escape attraction by a pillar. Colored arrows correspond to those in Figure 10A. (B), (C) Body pitch (blue) and bearing (red) (B) and phases of left (magenta) and right (black) hind legs (C) before, during, and after escape. Gray and green regions show pitching and turning phases. (D) A cuboidal robot traversing cluttered boulders using pitch-and-turn strategy. Colored arrows show motions defined in Figure 3. See Movies S8 (right) and S9 (right).
et al., 2019; Othayoth et al., 2020, 2021; Wang et al., 2021; Xuan and Li, 2020a), enabled by a potential energy landscape approach to locomotor transitions (Othayoth et al., 2020). Our results show that the attractive or repulsive interaction due to locomotor body shape is surprisingly insensitive to the geometry and size of rigid obstacles, the former being similar to those observed in legged robots traversing boulders (Qian and Goldman, 2016). Together, these findings suggest that there may exist general terrodynamic principles yet to be uncovered for complex 3D terrain. We speculate that our findings here also apply to compliant body interacting with compliant obstacles (Othayoth et al., 2020), because changes in stiffness only quantitatively changes the potential energy landscape but the topology is preserved.

Our minimalistic, quasi-static potential energy landscape is surprisingly useful in understanding the probabilistic dependence of locomotion on body shape, which results from complex body–obstacle interaction consisting of many small high-frequency collisions that challenge dynamic modeling. We envision potential energy landscape as the beginning of a statistical physics approach (analogous to (Onuchic and Wolynes, 2004)) to understanding locomotor–terrain interaction probabilistically without solving equations of motion (Othayoth et al., 2020). This is similar to how similar approaches have been successful in robotic grasping. We note that the motions here are only sensitive to the shape of the self-propelled moving body but not sensitive to the geometry of the rigid obstacles, which differs from robotic manipulation where motions are sensitive to the shape of both feeders and parts that move. Considering this, we speculate that physical interactions between two objects are only sensitive to the shape of the body/bodies that move.

We close with a discussion of future directions. First, our study mainly focused on two representative, static body shapes. Discovery of diverse terrodynamic shapes, control surfaces, and even morphing shapes (Li et al., 2017; Paik et al., 2012; Steltz et al., 2009) analogous to their aero/hydrodynamic counterparts (Fish and Lauder, 2017; Lentink et al., 2007; Stowers and Lentink, 2015) to modulate and adjust physical interaction will enable diverse locomotor transitions in robots (Li et al., 2015; Mintchev and Floreano, 2016; Miyashita et al., 2017; Roderick et al., 2017) required for broader applications. This will be facilitated by combining potential energy landscape modeling and composition of complex shapes using parameterizable shape primitives (Rosin, 2000). In addition, studies of interaction with diverse obstacles beyond the rigid pillars tested here will provide terrodynamic principles for traversing more heterogeneous terrain. Furthermore, it will be fruitful to model the animal’s active behavior (Wang et al., 2021) to understand the principles of how animals, and how robots should, locally sense and react to it (Arslan and Saranli, 2012) to make the desired locomotor transitions. This will be important in real-world missions with no global knowledge of the environment (Childers et al., 2016). Finally, future dynamic modeling that integrates potential energy landscape (which model conservative forces) with non-conservative forces and stochasticity will enable model-based, probabilistic shape optimization and provide a design tool for robots.

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Notes
1. Note that for this convention pitch is negative when the body pitches head up. However, we chose to report body pitch to be positive for head pitching up to be consistent with common definition of pitching up.
2. In the animal panels, the probabilities of modes and outcomes shown do not sum to 100%. This was because modes that were not our focus were not shown. In these trials (e.g., 18% of all trials in Figure 3C and 6% in Figure 3D), after initial contact, the animal either contacted the sidewalls, substantially slowed down using active sensory feedback, or stopped moving.

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Supplemental material
Supplemental material for this article is available online.

References


Li C, Pullin AO, Haldane DW, et al. (2015) Terradynamically streamlined shapes in animals and robots enhance...
traversability through densely cluttered terrain. *Bioinspiration and Biomimetics* 10(4): 46003.


Supplementary Information for

Shape-induced obstacle attraction and repulsion during dynamic locomotion

Yuanfeng Han, Ratan Othayoth, Yulong Wang, Chun-Cheng Hsu, Rafael de la Tijera Obert, Evains Francois, Chen Li*

*Corresponding author (chen.li@jhu.edu)

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Supplementary Text S1 to S5
Supplementary References
Supplementary Figures S1 to S8
Legends for Supplementary Movies S1 to S13

Other supplementary materials for this manuscript include the following:

Supplementary Movies S1 to S13
Supplementary Tables

Table S1. Sample size, mass, and dimensions of robot experiments. Average data are mean ± s.d.

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Supplementary Text

S1. Details of imaging and 3-D reconstruction

We used a small shutter time (500 µs) to reduce motion blur and a small lens aperture to maximize the focal depth of field. We illuminated the test area with four 1000 W work lamps. We calibrated the cameras for 3-D kinematics reconstruction via Direct Linear Transformation (Hedrick, 2008). The custom calibration object built from Lego bricks covered the entire field of view for maximal reconstruction precision. We verified tracking and reconstruction fidelity (s.d. of position error = 0.6 mm; s.d. of orientation error = 1.1°) using a 3-D printed high precision object. We also verified that lens distortion was minimal (<1%) using the checkboard distortion measurement method. We verified that the reconstructed 3-D motion matched with the observed motion by projecting it onto videos from each camera.

S2. Statistics

All the probability values were calculated relative to the total number of accepted trials of each treatment. All average data are reported as means ± 1 s.d.

For both robot and animal, we performed Kruskal-Wallis tests to check statistical significance ($\alpha = 0.05$) of the following dependencies:

1. traversal probability on obstacle shape and orientation, for each body shape;
2. final bearing on initial bearing, for each body shape and obstacle shape and orientation treatment;
3. maximal pitch increase on initial bearing, for each body shape and obstacle shape and orientation treatment;
4. final bearing on body shape and obstacle shape and orientation treatment;
5. maximal pitch increase on body shape and obstacle shape and orientation treatment;
6. difference in final bearing between animal and robot, for each body shape and obstacle shape and orientation treatment;
(7) difference in maximal pitch increase between animal and robot, for each body shape and obstacle shape and orientation treatment;
(8) distance along trajectory travelled on body shapes in multi-pillar robot experiments (Section 6.1)
(9) difference in speed, deceleration, and absolute angular acceleration between intact and sensor-deprived animals (Section S3).

For the animal, we pooled data from all individuals and included individual as a random effect in statistical tests.

**S3. Animal’s initial interaction is dominated by passive mechanics**

Because cockroaches can use antennae to sense and detect obstacles to navigate complex terrain (Cowan et al., 2006; Harley et al., 2009; Okada and Toh, 2006), it is possible that obstacle interaction is dominated by sensory feedback control rather than passive mechanical interaction (Dickinson et al., 2000). To verify that this was not the case, we compared the magnitudes of speed, acceleration, and angular acceleration in the horizontal plane at initial collision for the same individuals before and after depriving them of antennae (Harley et al., 2009). None of these differed (Fig. S3; \( P > 0.05 \), Kruskal-Wallis test), indicating that the effect of sensory feedback control was minimal at initial contact. In addition, body pitch, yaw, and roll changed little after the antennae came in range of the obstacles before initial collision, indicating that the animal did not actively slow down further or reorient its body before collision (Fig. S2). Even after initial collision, response by the animal is delayed (~90 ms) due to delays in sensory signal transmission (40 ms (Harley et al., 2009)) and subsequent leg muscle activation (47 ms (More et al., 2010; Sponberg and Full, 2008)). Thus, the animal’s initial body-obstacle interaction was mostly feedforward and dominated by passive mechanics and thus behaved similarly to the feedforward robot. It was not until the later part of interaction phase (average duration: \( 130 \pm 110 \) ms) that the animal adjusted its body motion to escape obstacle attraction (Figs. 4D, 5D, S5F, S6F).
S4. Body-obstacle interaction consists of continual collisions

We found that body-obstacle interaction during dynamic interaction consisted of stochastic continual collisions for both animal and robot. This could be observed from body-obstacle distance, which fluctuated substantially (up to 10% body length) and irregularly about several times per second (Fig. S1A, B), with standard deviation exceeding the mean (Fig. S1C). In addition, we verified that even when interacting with a single pillar, the robot suffered large unpredictable rotational fluctuations (Fig. S2).

S5. Application to aerial robots

Although discovered for terrestrial locomotion, the principles of shape-induced obstacle attraction and repulsion may also be useful for aerial or aquatic locomotion where the body physically interact with solid objects. As a proof of concept, we tested a small, off-the-shelf drone with a custom compliant cage (Fig. S8, Movie S13). When encountering a narrow spacing between two vertical pillars (110% cage width), the drone with a cuboidal cage (Fig. S8D, 10 trials) was always attracted towards the pillar it first contacted and was frequently stuck between the two pillars. By contrast, with an elliptical cage (Fig. S8B, E), it was always repelled away from the pillars into the gap and always traversed. In addition, obstacle attraction induced by the cuboidal shape enabled the drone to be perch onto a pillar (via Velcro) (Fig. S8C, F). Although drones with spherical protective cages have been demonstrated to use collisions to traverse sparse obstacles (Briod et al., 2013, 2014), our demonstration showed that desired obstacle interactions can be elicited using body shape and will be useful for aerial robots to traverse extremely cluttered environments.

Supplementary References


Fig. S1. **Body-obstacle interaction consists of continual collisions.** (A) Body-obstacle distance (in units of body length). All experimental trials are pooled onto the same time axis. Horizontal black line shows threshold of 2% body length to classify contact and non-contact. (B) Average contact frequency. (C) Coefficient of variation of body-obstacle distance (s.d./mean). Blue and red are for cuboidal and elliptical body shapes, respectively.
Fig. S2. Robot orientation varies substantially during obstacle interaction. (A, B) Body yaw, pitch, roll of cuboidal (A) and elliptical (B) robot in absolute values. Error bars show ± 1 s.d.
Fig. S3. Animal's initial body-pillar collision is dominated by passive mechanics and not sensory feedback. Comparison of (A) speed, (B) acceleration, and (C) angular (turning) acceleration in the horizontal (x-y) plane of the same individuals before and after removing both antennae. Error bars show ± 1 s.d. Brackets and n.s. indicate no significant difference.
**Fig. S4.** Traversal probability for square pillars. Solid bars are for robot and empty bars are for animal. Blue is for cuboidal body and red is for elliptical body. Horizontal, vertical, and oblique hatches are for square pillars oriented at 0°, 30°, and 60° relative to x-axis. Error bars show ± 1 s.d. See Movie S2 for representative trials.
Fig. S5. Turning motion during obstacle interaction for square pillars. See Fig. 4 for definition of plots in (A, C-F). See Fig. S4 for definition of bar graph in (B). See Table 1 for sample size. See Movie S2 for representative trials.
Fig. S6. Pitching motion during obstacle interaction for square pillars. See Fig. 5 for definition of plots in (A, C-F). See Fig. S4 for definition of bar graph in (B). See Table 1 for sample size. See Movie S2 for representative trials.
Fig. S7. Potential energy landscape with square pillars of different orientations. (A-C) Cuboidal and (D-E) elliptical robot interacting with square pillars oriented at $0^\circ$ (A, D), $30^\circ$ (B, E), and $60^\circ$ (C, F) relative to $x$-axis. See Fig. 6 for definition of plots.
Fig. S8. Drone using body shape-induced obstacle attraction and repulsion. (A) Failure to traverse a gap between two pillars using a cuboidal body. (B) Gap traversal using an elliptical body. (C) Perching onto a pillar using a cuboidal body. Red curve shows drone trajectory. (D, E, F) Body turning direction (rectangular boxes) and outcome (rounded boxes) for cases shown in (A-C). Dashed body shows typical state at initial contact and solid body shows typical state resulting from interaction. Numbers next to the arrows show probability of that transition. See Table 1 for sample size.
Supplementary Movies

**Movie S1.** Body motion when interacting with a pillar obstacle.

**Movie S2.** Effect of body shape on interaction is insensitive to obstacle shape and orientation.

**Movie S3.** Potential energy landscape of a cuboidal body interacting with a pillar obstacle.

**Movie S4.** Potential energy landscape of an elliptical body interacting with a pillar obstacle.

**Movie S5.** Ensemble of system state trajectories on potential energy landscape with a cuboidal body.

**Movie S6.** Ensemble of system state trajectories on potential energy landscape with an elliptical body.

**Movie S7.** Potential energy landscape of intermediate body shapes between elliptical and cuboidal.

**Movie S8.** Robot moving in cluttered terrain.

**Movie S9.** Cuboidal robot moving in natural cluttered terrain using open-loop gait vs. pitch-and-turn strategy.

**Movie S10.** Robot traversing natural cluttered terrain using passive control via shape and active pitch-and-turn strategy.

**Movie S11.** Potential energy landscape predicts turning torque required for a cuboidal body to overcome that from body weight to escape obstacle attraction.

**Movie S12.** Pitching up helps a cuboidal robot turn to escape obstacle attraction.

**Movie S13.** Drone traversing a narrow obstacle gap and perching onto an obstacle using passive control via body shape.